

Stat 201: Introduction to Statistics

Standard 4: Graphical Summaries

Chapter Two

Summaries

Graphical Displays

Variable Type	Graphical Display	Numerical Summary
Categorical	Pie chart or bar graph	Frequency table
Quantitative	Histogram or box plot – can also try dotplot or stem & leaf	Quantitative Summary
1-Categorical and 1-Quantitative	Side by Side boxplots	Quantitative Summary for groups
2-Categorical	Side by side pie charts or bar graphs best: stacked bar chart	Contingency Table or side by side frequency tables
2-Quantitative	Scatter plot	Side by side Quantitative Summaries

Misrepresentation of Data

- You should be able to look at your graphs and realize when you've made a mistake
 - The percentages of all relative frequency graphs should add to 1 or 100%
 - The scale should be understandable and constant
 - Consider whether or not you need to start your y axis at zero or caution against misreading the graph
 - Graphs should be simple and easy to interpret correctly in just a few moments.

Variable

```
graph TD; Variable[Variable] --> Categorical[Categorical]; Variable --> Quantitative[Quantitative]; Quantitative --> Discrete[Discrete]; Quantitative --> Continuous[Continuous];
```

Categorical

- pie chart (few groups)
- bar graph(many groups)

Quantitative

Discrete

- dot plot (few values)
- bar graph(make values groups)
- boxplot (for many values)
- histogram (for many values)

Continuous

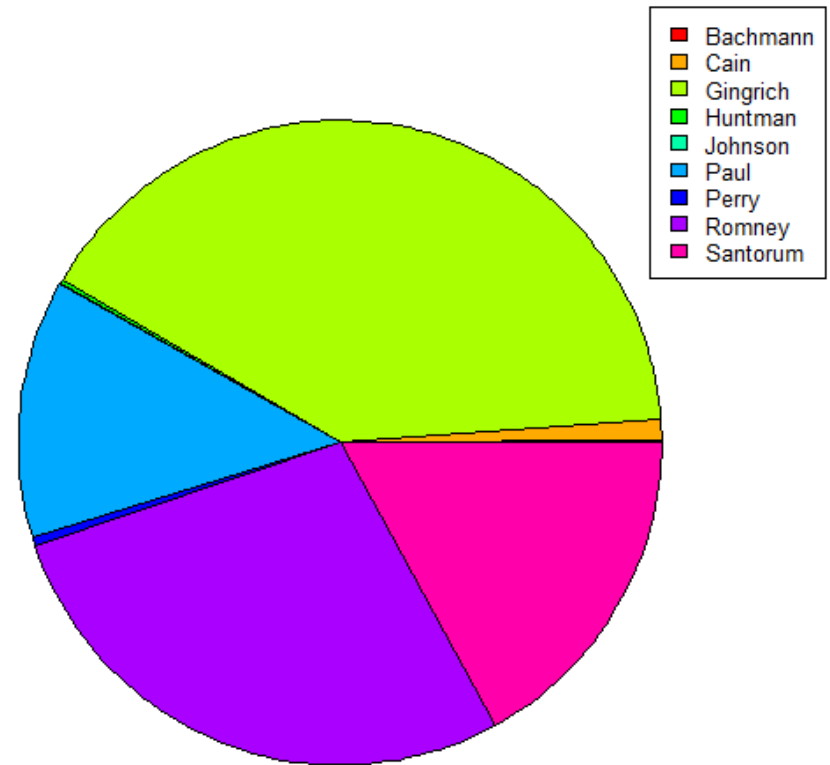
- box plot
- histogram

Walkthrough

Summarizing Qualitative Data: Pie Chart

Number of Votes for Candidates in 2012 SC Primary

- Useful when there are a small number of categories



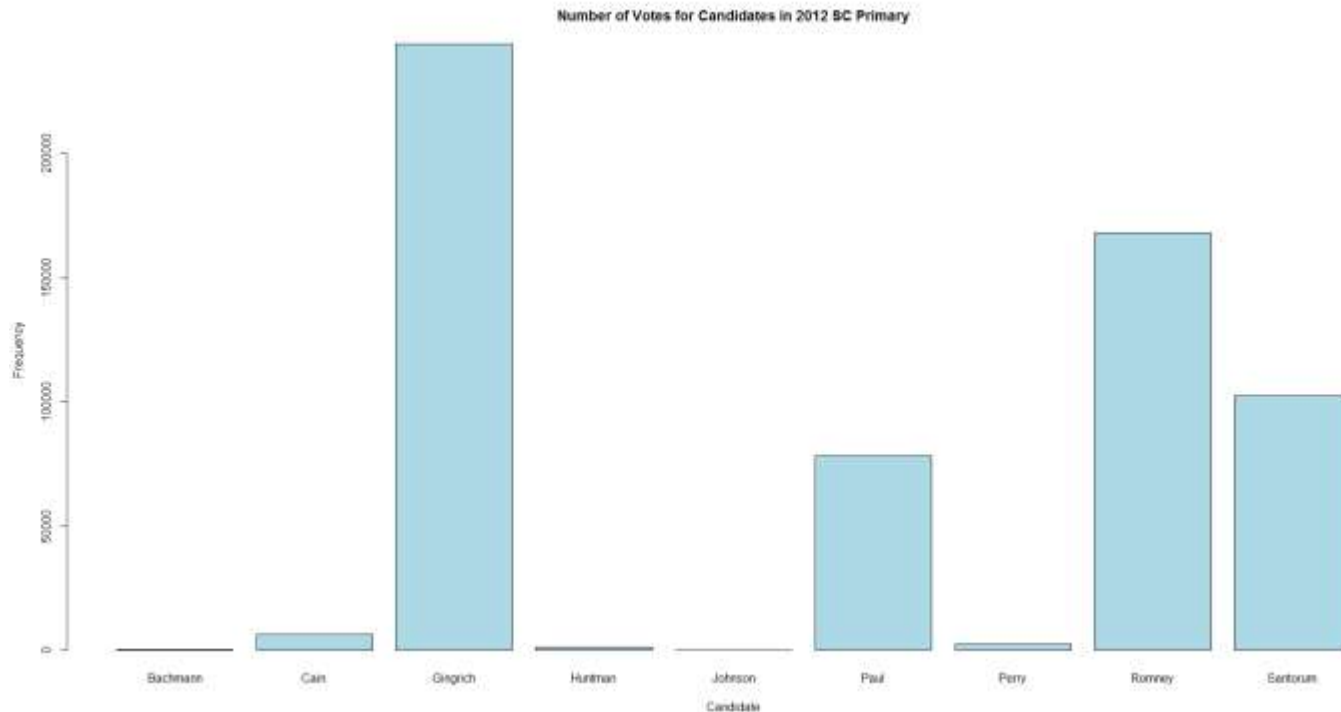
Data: Graphical Summary

- **StatCrunch Command:**

Graph → Pie Chart → w/data → Select your variable(s) → Compute

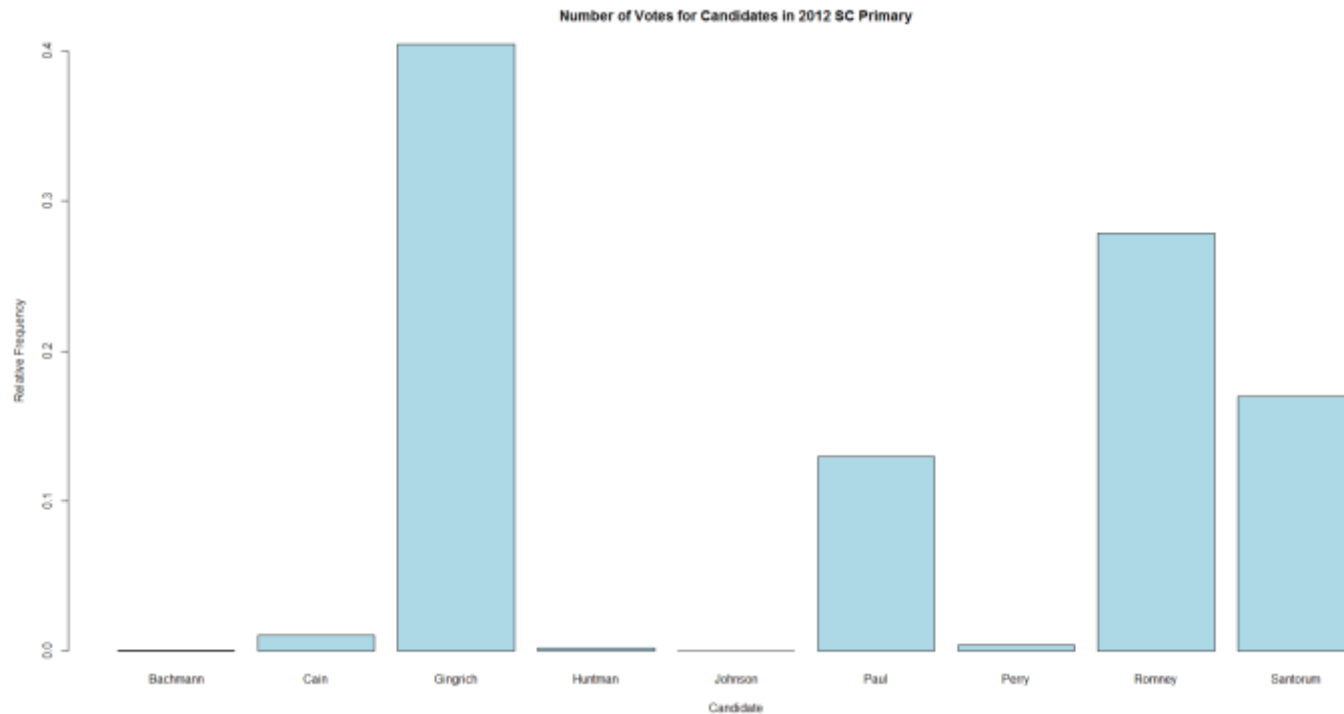
Summarizing Qualitative Data: Bar Graph

- Useful when there are many categories of the variable
- Useful to compare groups



Summarizing Qualitative Data: Bar Graph

- **Note:** the relative frequency chart has the same shape but a different y-axis



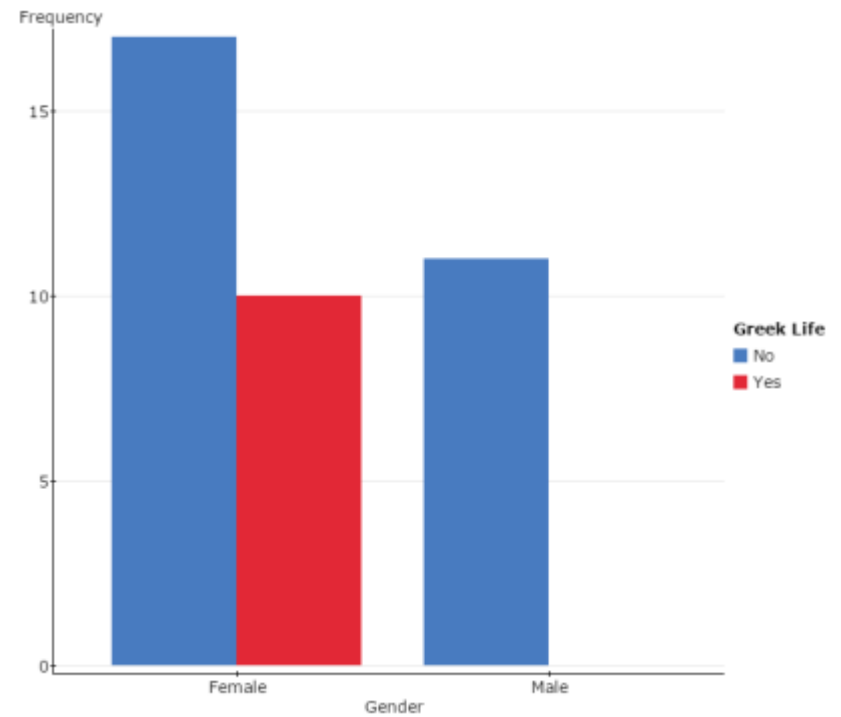
Data: Graphical Summary

- **StatCrunch Command:**

Graph → Bar Plot → w/data → Select your variable(s) → Compute

Categorical Summary: Side by Side Bar Graph

- We could draw bar graphs side by side to compare the data for the two different groups.



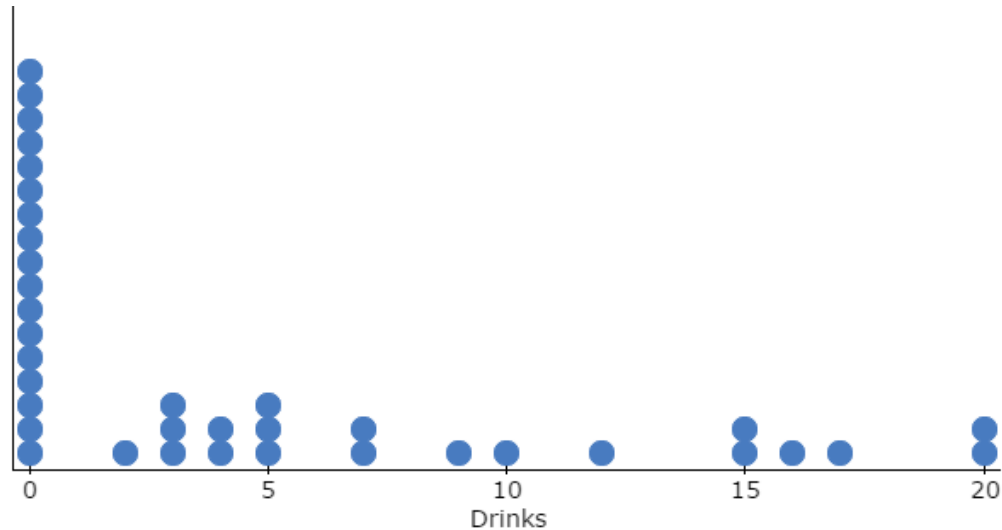
Data: Graphical Summary

- **StatCrunch Command:**

Graph → Bar Plot → w/data → Select the variable you'd like on the x-axis → Group by the variable you would like the bars to be split by → Compute

Quantitative Summary: Dot Plot

- Useful for smaller datasets
- Useful for finding outliers
- I don't like these – histograms are **almost** always better



Data: Graphical Summary

- **StatCrunch Command:**

Graph → Dot Plot → w/data → Select the variable(s) → Compute

Quantitative Summary: Stem and Leaf

- Retains actual data values

Example: Number of calories for a large serving of French Fries at Fast Food Restaurants
(source: <http://www.acaloriecounter.com/fast-food.php>)

570	500	500	540	566	631	610
400	400	640	550	700	280	380
480	430	370	380	490	310	620
450	730	260				

Stem Unit = hundreds, Leaf Unit = Tens

Variable: Calories

2: 68

3: 1788

4: 003589

5: 004577

6: 1234

7: 03

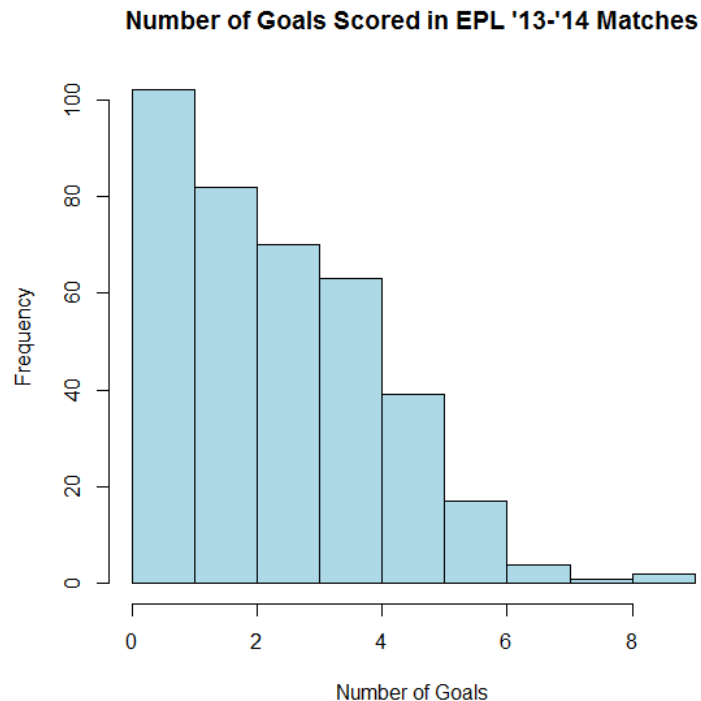
Data: Graphical Summary

- **StatCrunch Command:**

Graph → Stem and Leaf → Select the variable(s) → Compute

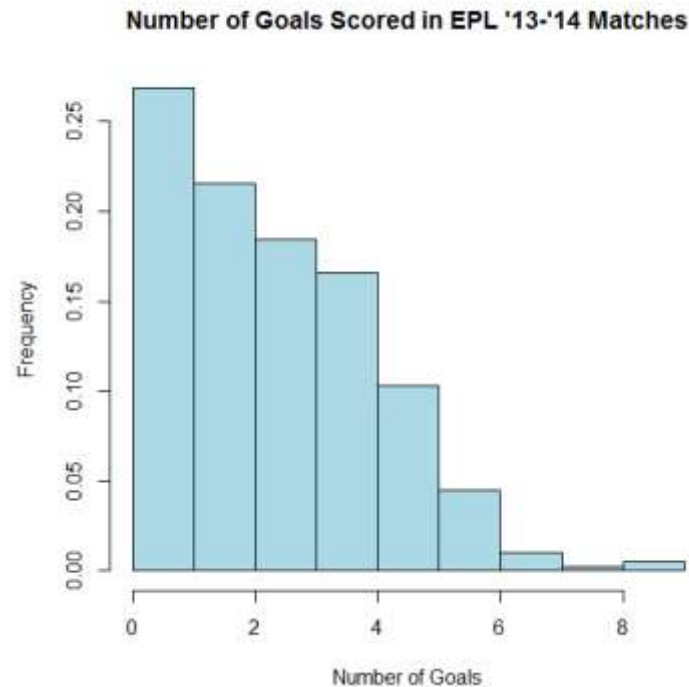
Summarizing Quantitative Data: Histogram

- Histograms are used to summarize quantitative data and will be our main tool for continuous data



Summarizing Quantitative Data: Histogram

- **Note:** the relative frequency chart has the same shape but a different y-axis



Data: Graphical Summary

- **StatCrunch Command:**

Graph → Histogram → Select the
variable(s) → Compute

Histograms Vs. Bar Charts

- With bar charts, each column represents a group defined by a categorical variable
- With histograms, each column represents a group defined by a quantitative variable.

Histograms Vs. Bar Charts

- With bar charts, each column represents a group defined by a class of a qualitative (categorical) variable
- With histograms, each column represents a group defined by a quantitative variable. R will automatically generate classes for the quantitative data

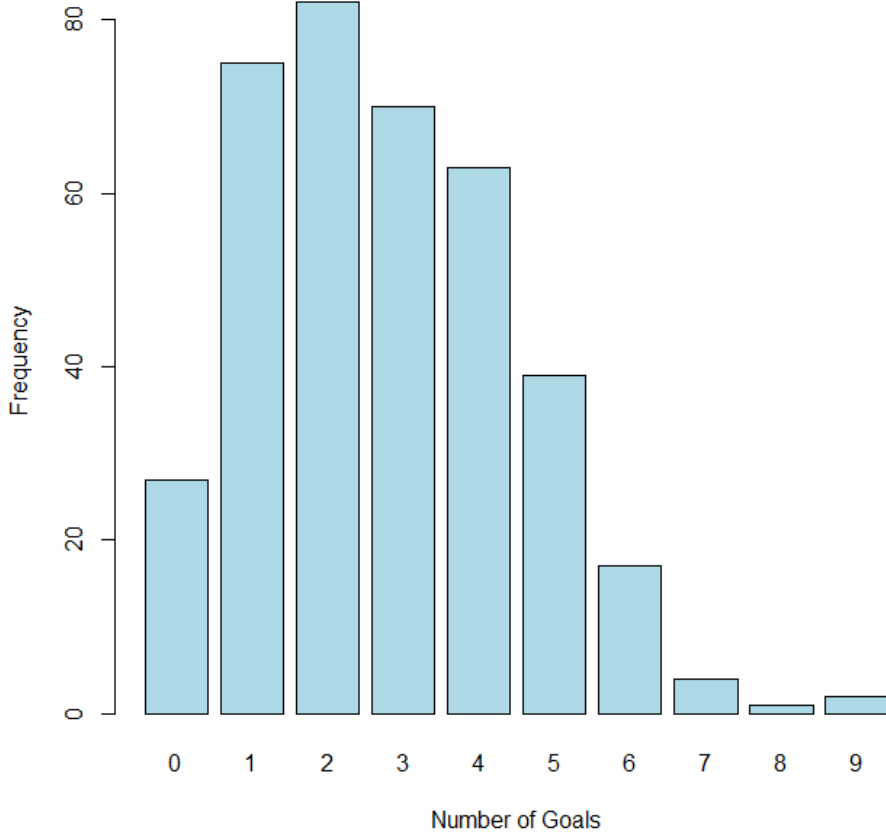
Histograms Vs. Bar Charts

- In our example of EPL goals over the '13-'14 season the groups that R creates for the histogram are as follow

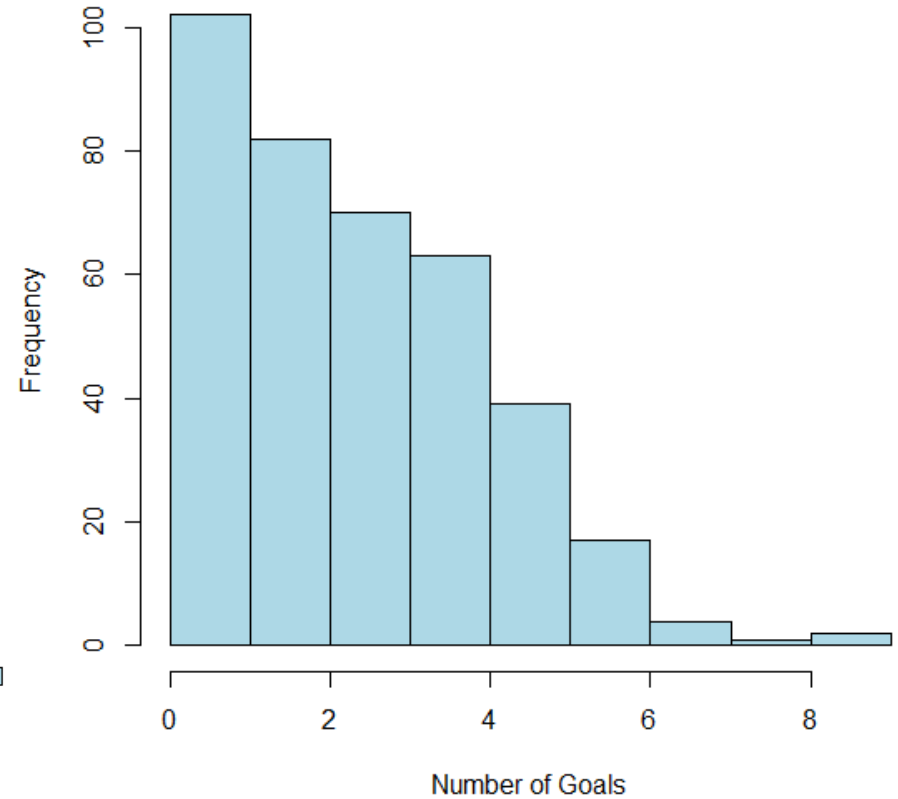
[0,1]	102
(1,2]	82
(2,3]	70
(3,4]	63
(4,5]	39
(5,6]	17
(6,7]	4
(7,8]	1
(8,9]	2

Histograms Vs. Bar Charts

Number of Goals Scored in EPL '13-'14 Matches



Number of Goals Scored in EPL '13-'14 Matches



Histograms Vs. Bar Charts

- In this case, because there are so few observable values the histogram is actually a little misleading – it just combines the bars at 0 and 1 and the rest is the same as the bar plot

Summarizing Quantitative Data: Histograms

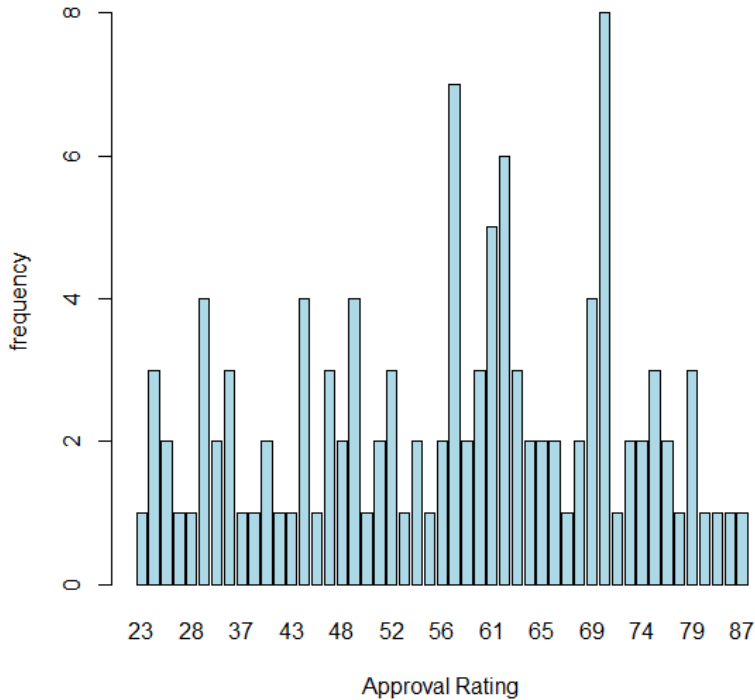
- Let's consider a different dataset – as we mentioned earlier, the small number of observable values allows us to use the qualitative(categorical) approach with this EPL data
- We will continue looking at histograms by considering the discrete quantitative data considering the quarterly presidential approval ratings from '54 to '74

Summarizing Quantitative Data: Histograms

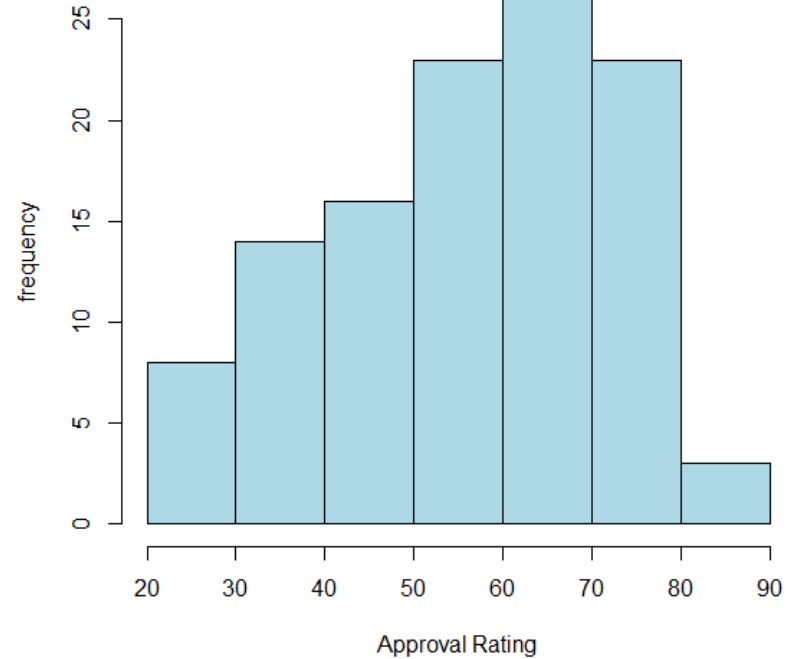
- Among the quarterly presidential approval ratings there are 49 observable values ranging from 23 (Truman in '51) to 87(Truman in '45)
- Here, if we followed what we did for qualitative (categorical data) we would find a frequency table with 49 rows and a bar graph with 49 bars
- Here a histogram is easily a better visual

Summarizing Quantitative Data: Histograms

Quarterly Presidential Approval Ratings



Quarterly Presidential Approval Ratings



Histograms Vs. Bar Charts

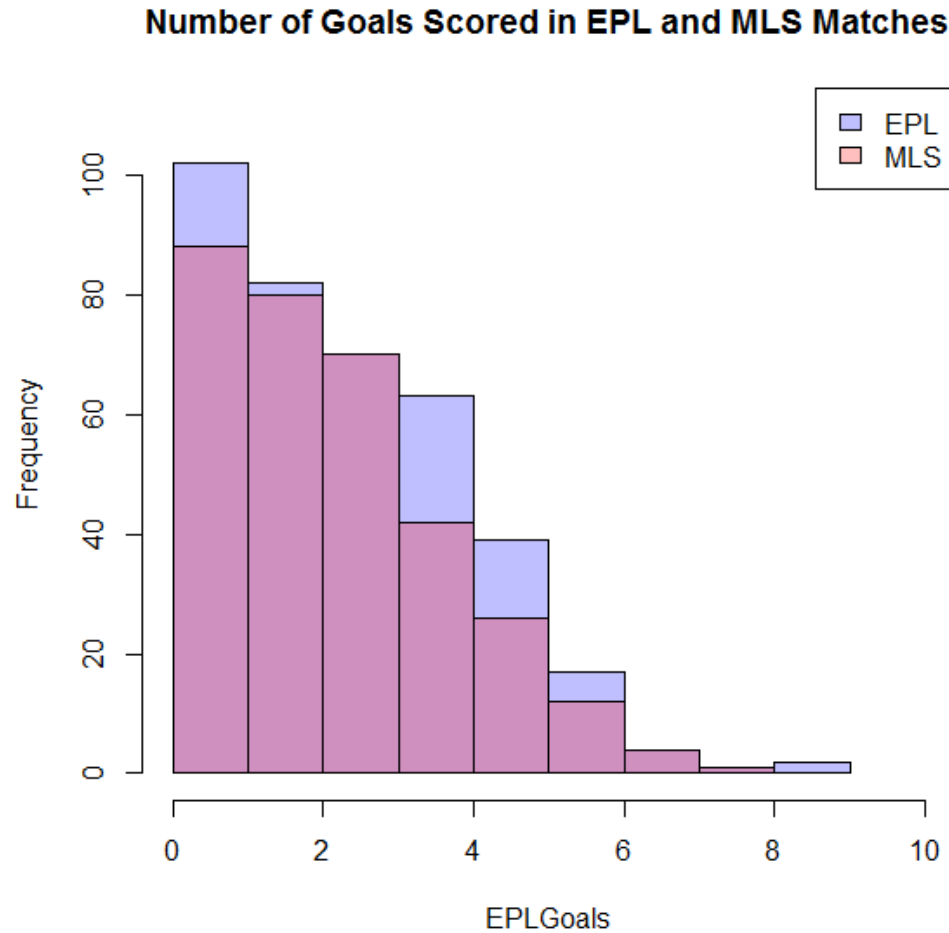
- In our example of Presidential approval ratings the groups that R creates for the histogram are as follow:

[20,30]	8
(30,40]	14
(40,50]	16
(50,60]	23
(60,70]	27
(70,80]	23
(80,90]	43

Talking about Two Things at Once

- In many cases we're looking at two groups and comparing them.
- Here we consider the EPL goals data and compare it to another league to see if teams score more or less over their season
- The following graphs compare goals in the EPL '13-'14 season and goals in the MLS '13 season

Talking about Two Things at Once

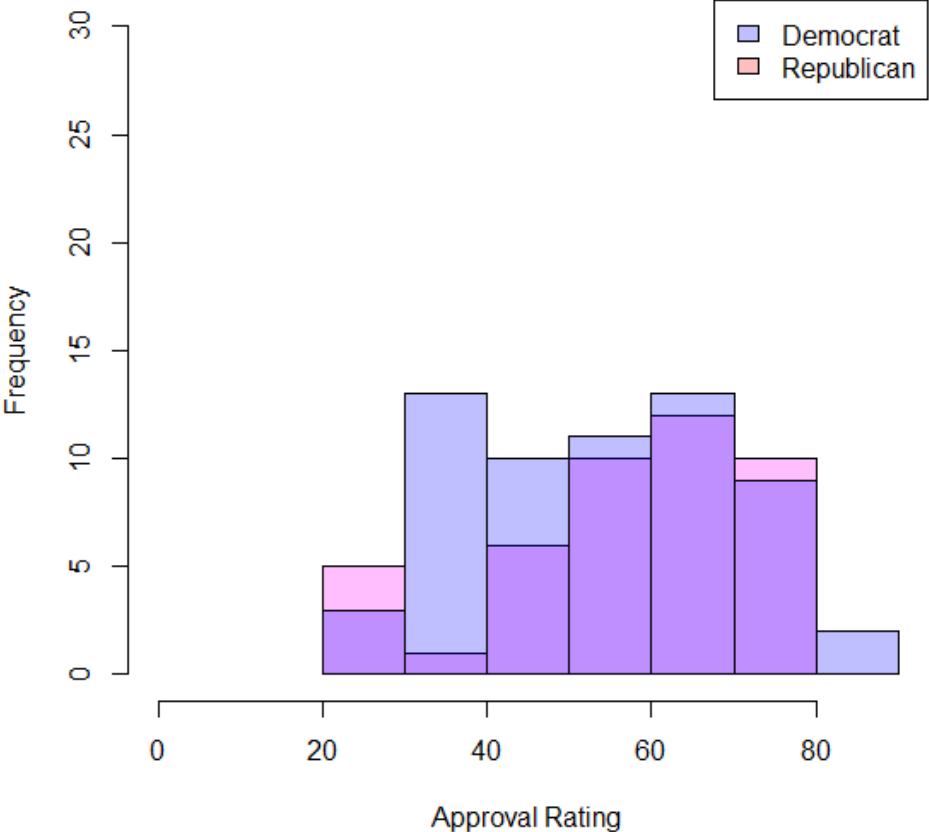


Talking about Two Things at Once

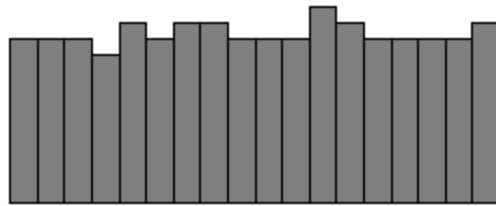
- Here, we consider the presidential approval data and split it into democratic and republican presidents to compare the two parties ratings
- The following graphs compare quarterly ratings of republican and democrat presidents

Talking about Two Things at Once

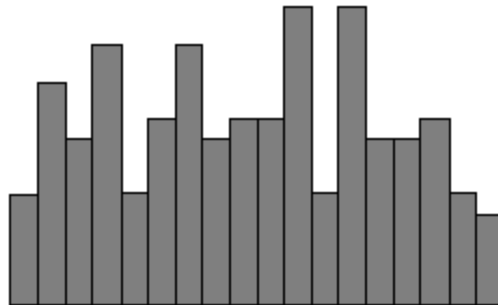
Quarterly Presidential Approval Ratings



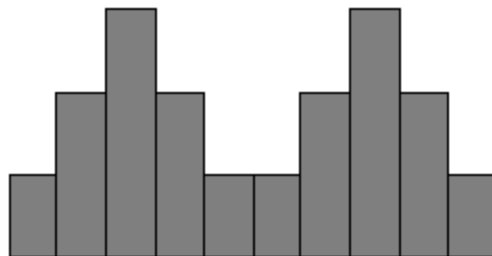
Quantitative Summary: Histogram Shapes



Uniform

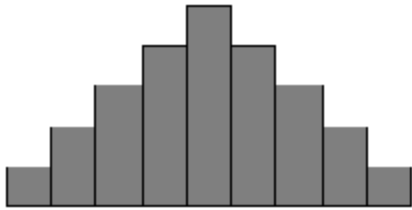


Random



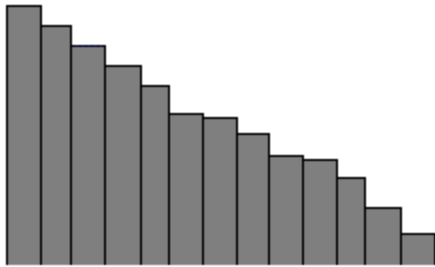
Bimodal

Quantitative Summary: Histogram Shapes



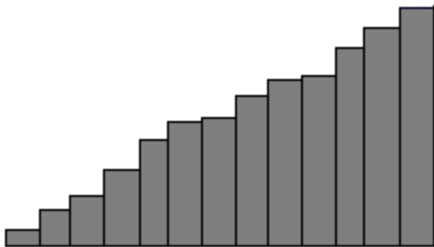
Bell-shaped - Unimodal

mean \approx median



Skewed Right

mean $>$ median

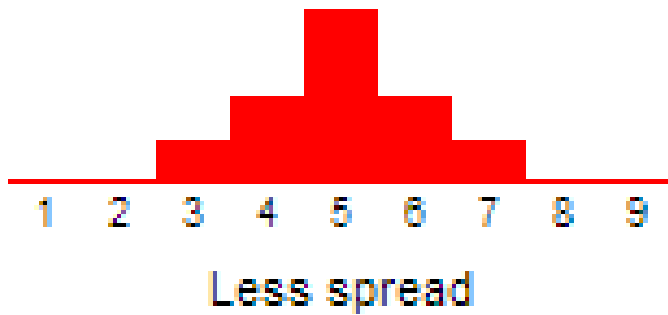


Skewed Left

mean $<$ median

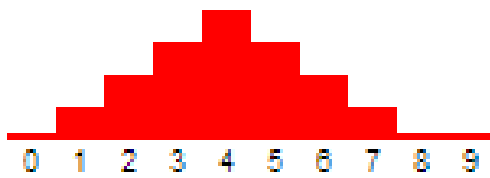
Histogram

- Spread:

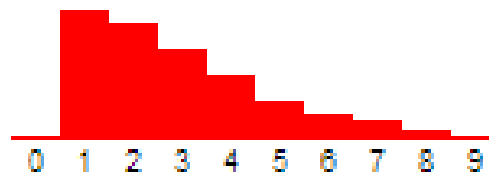


Histogram

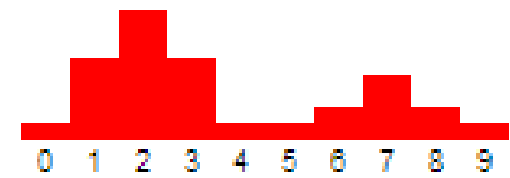
- Shape:



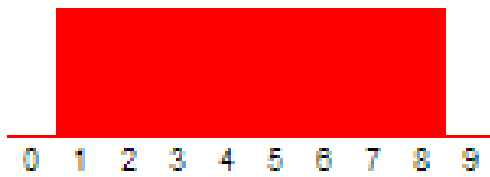
Symmetric, unimodal,
bell-shaped



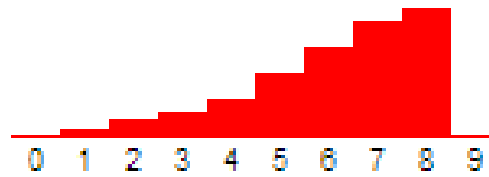
Skewed right



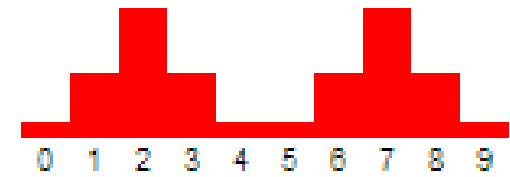
Non-symmetric, bimodal



Uniform



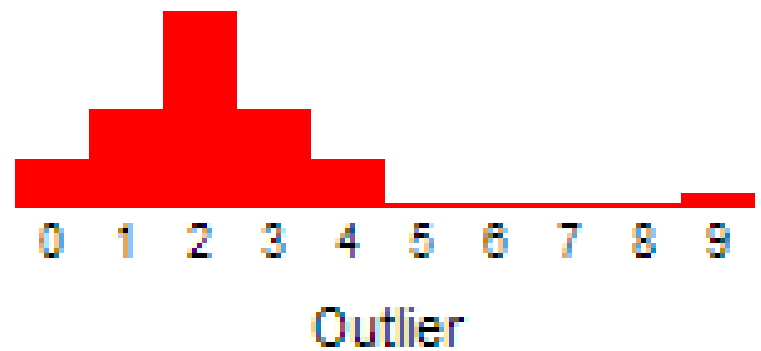
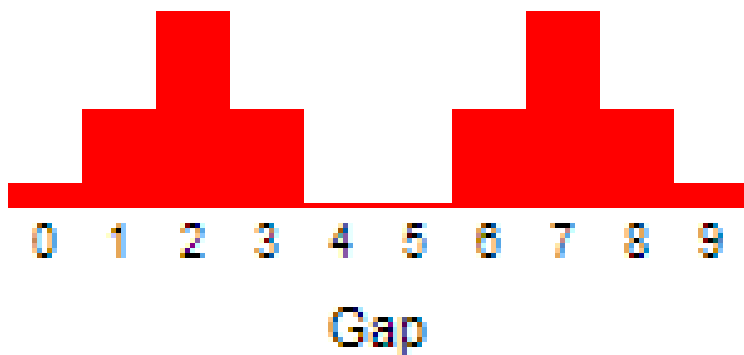
Skewed left



Symmetric, bimodal

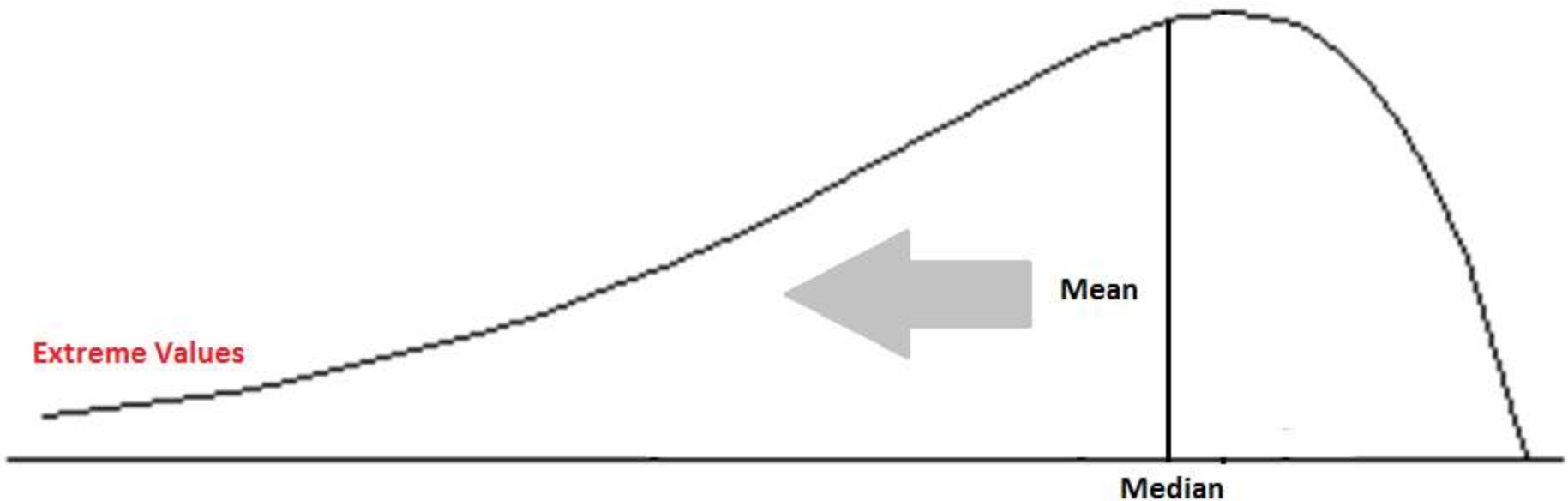
Histogram

- Gap vs. Outlier:



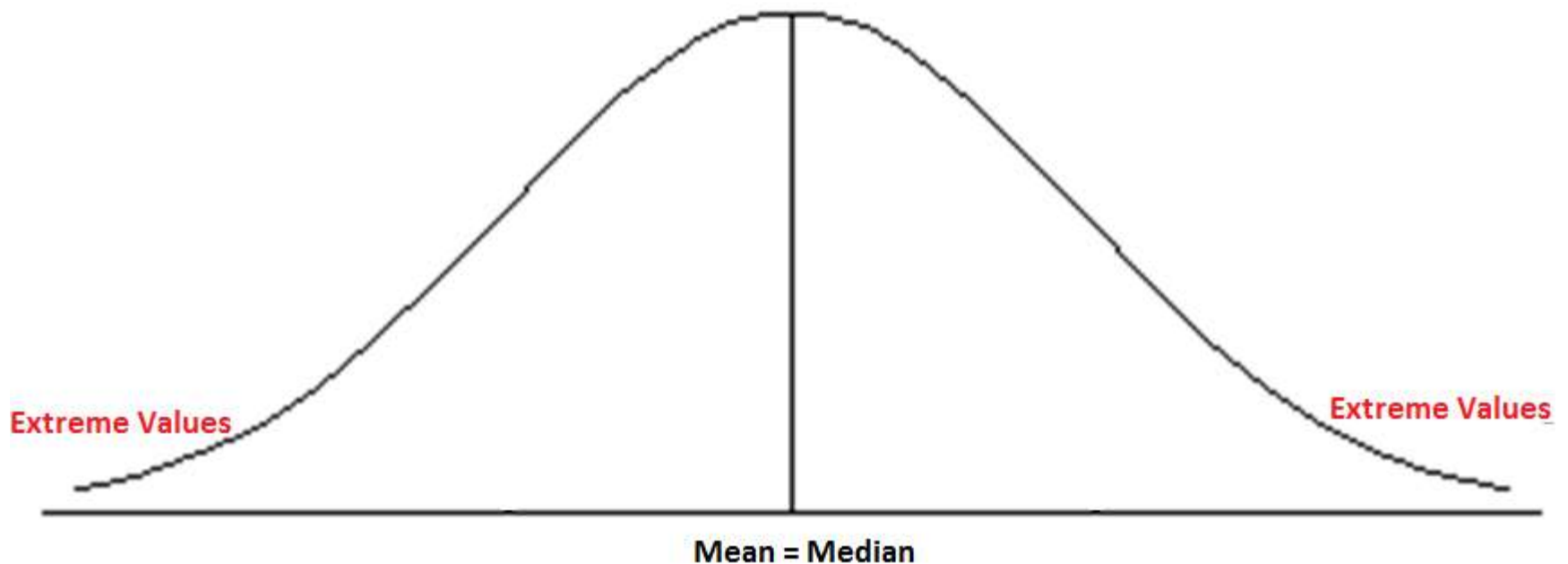
Quantitative Summary: Histograms – Left Skewed

- Here we see a left skewed graph – the extreme values on the left drag the mean to the left tail causing $\text{Mean} < \text{Median}$



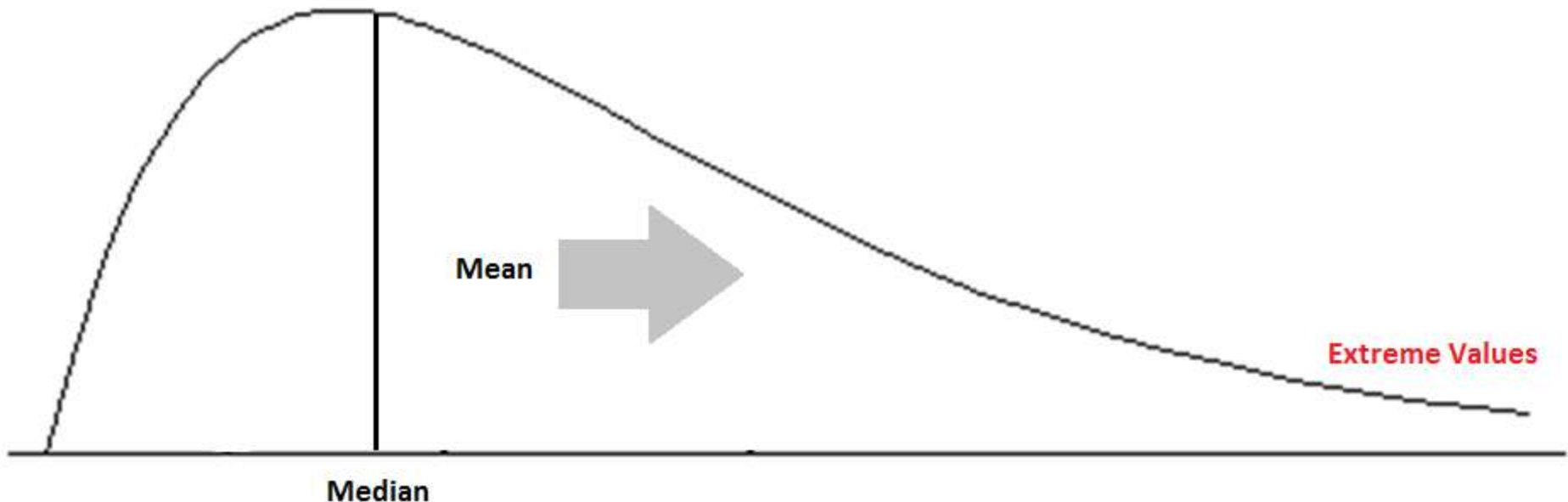
Quantitative Summary: Histograms – Bell Shaped

- Here there is no skew – the extreme values on both side cancel any outlying effect on the mean

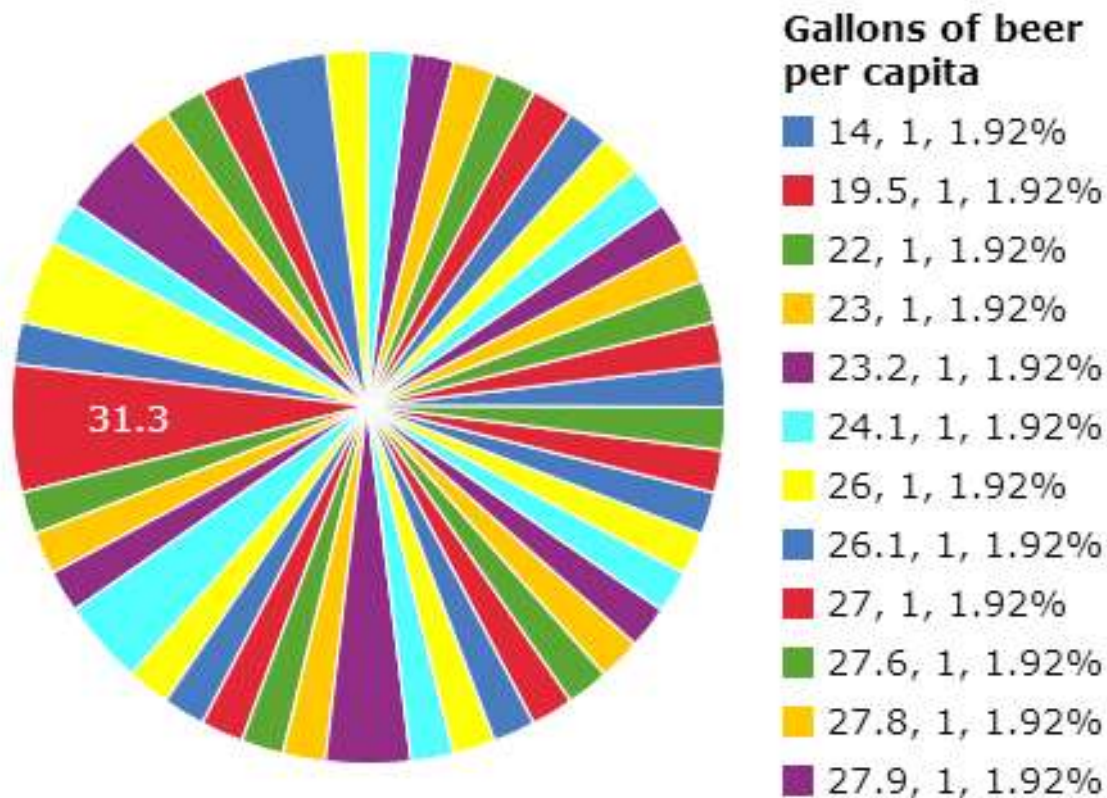


Quantitative Summary: Histograms – Left Skewed

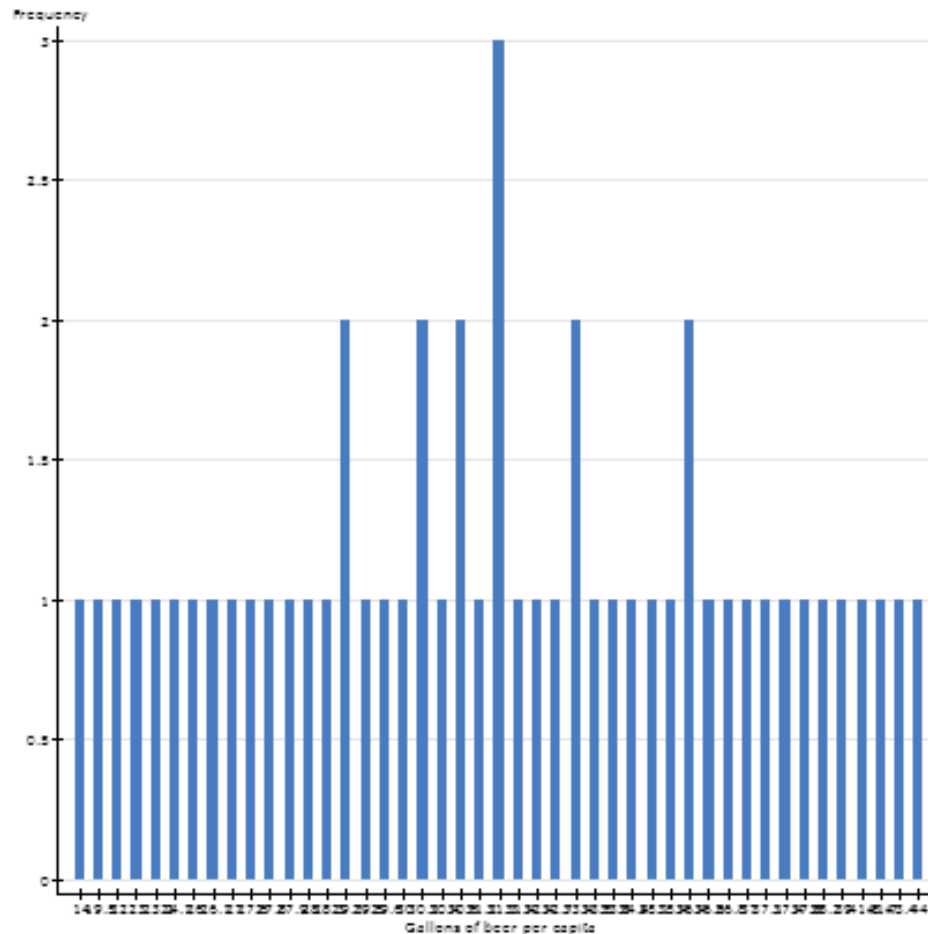
- Here we see a right skewed graph – the extreme values on the right drag the mean to the right tail causing $\text{Mean} > \text{Median}$



Remember: With graphs, if it's ugly
it's probably not right.



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Misrepresentation of Data

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